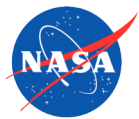


# Optimal Estimation Retrieval of CO<sub>2</sub> from AIRS spectra

Bill Irion

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With thanks to Susan Sund-Kulawik, John Worden,  
Kevin Bowman, Mike Gunson and Luke Chen



National Aeronautics and  
Space Administration

Jet Propulsion Laboratory  
California Institute of Technology  
Pasadena, California



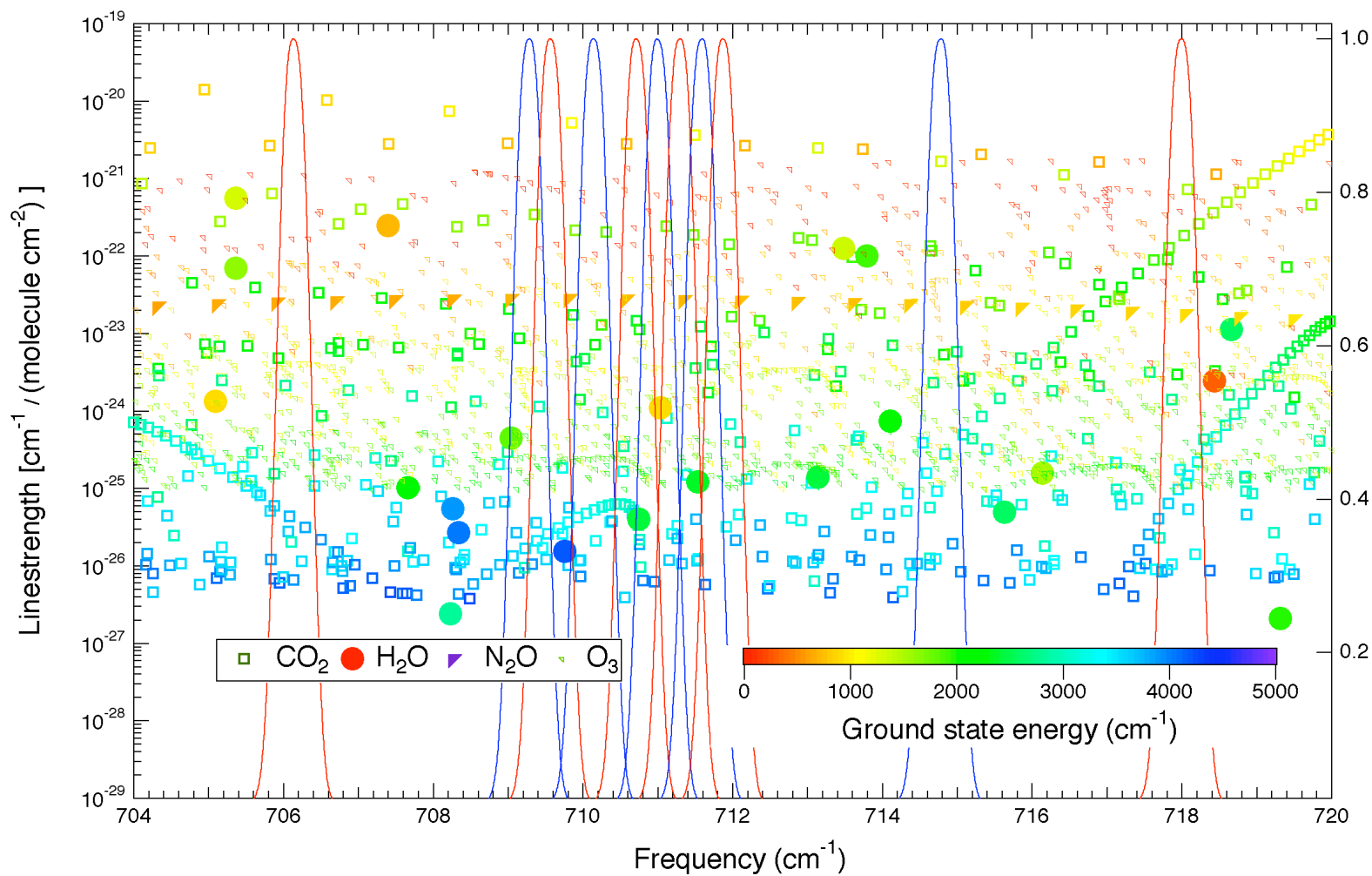
# Goals:

- Develop a method using Optimal Estimation (OE) techniques (including constraints) to retrieve upper tropospheric CO<sub>2</sub>.
- Compare retrievals with Vanishing Partial Derivatives (VPD) results.
- Emphasis is on *distribution* of results
  - Biases possible between OE and VPD because of different forward models and re-retrieval of temperature and water vapor profiles

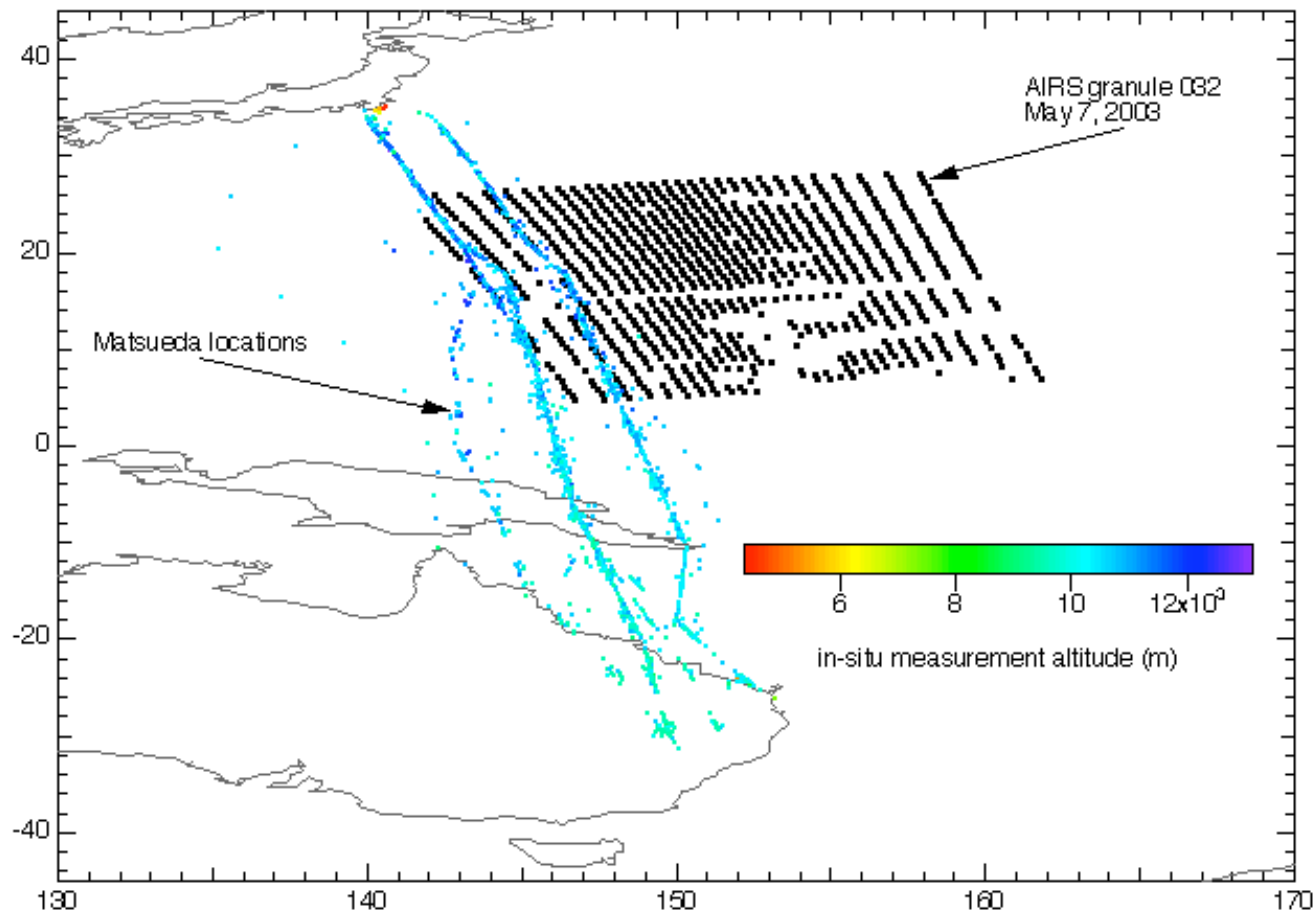
# Methodology:

- TES code and forward model.
- AIRS cloud-cleared radiances.
- Temperature and water vapor profiles retrieved prior to CO<sub>2</sub> retrieval.
- Water and ozone simultaneously retrieved as “interferent gases” in CO<sub>2</sub> retrieval.

# What's in the window?



# Measurement location



*Noisy measurement for AIRS so we need to average results*

# Optimal Estimation Cost Function

$$\begin{aligned} C &= \min_x \left( (\mathbf{y} - F(\mathbf{x})) \mathbf{S}_n^{-1} (\mathbf{y} - F(\mathbf{x}))^T + (\mathbf{x} - \mathbf{x}_c) \mathbf{\Lambda} (\mathbf{x} - \mathbf{x}_c)^T \right) \\ &= \min_x \left( \|\mathbf{y} - F(\mathbf{x})\|_{\mathbf{S}_n^{-1}}^2 + \|\mathbf{x} - \mathbf{x}_c\|_{\mathbf{\Lambda}}^2 \right) \end{aligned}$$

$\hat{\mathbf{x}}$  = retrieved state       $\mathbf{x}$  = true state

$\mathbf{x}_c$  = first guess       $\mathbf{y}$  = observed radiance

$F(\mathbf{x})$  = forward model       $\mathbf{S}_n^{-1}$  = noise covariance matrix

$\mathbf{\Lambda}$  = constraint matrix (usually inverse of a priori covar matrix)

# Optimal Estimation Cost Function

$$C = \min_x \left( (\mathbf{y} - F(\mathbf{x})) \mathbf{S}_n^{-1} (\mathbf{y} - F(\mathbf{x}))^T + (\mathbf{x} - \mathbf{x}_c) \Lambda (\mathbf{x} - \mathbf{x}_c)^T \right)$$
$$= \min_x \left( \|\mathbf{y} - F(\mathbf{x})\|_{\mathbf{S}_n^{-1}}^2 + \|\mathbf{x} - \mathbf{x}_c\|_{\Lambda}^2 \right)$$

$\hat{\mathbf{x}}$  = retrieved state

$\mathbf{x}$  = true state

$\mathbf{x}_c$  = first guess

$\mathbf{y}$  = observed radiance

$F(\mathbf{x})$  = forward model     $\mathbf{S}_n^{-1}$  = noise covariance matrix

$\Lambda$  = constraint matrix (usually inverse of a priori covar matrix)

*What to choose for constraint?*

# An ad hoc covariance/constraint

Note that we're retrieving a  $\ln(\text{mixing ratio})$  profile

On the diagonal:

$$S_{i,i} = \left[ \ln \left( \frac{\beta - 0.01}{1 + 0.03(z/\delta z)} + 1.01 \right) \right]^2$$

$\beta$  is the fractional std. dev. at surface

$z$  = altitude

$\delta z$  = vertical spacing

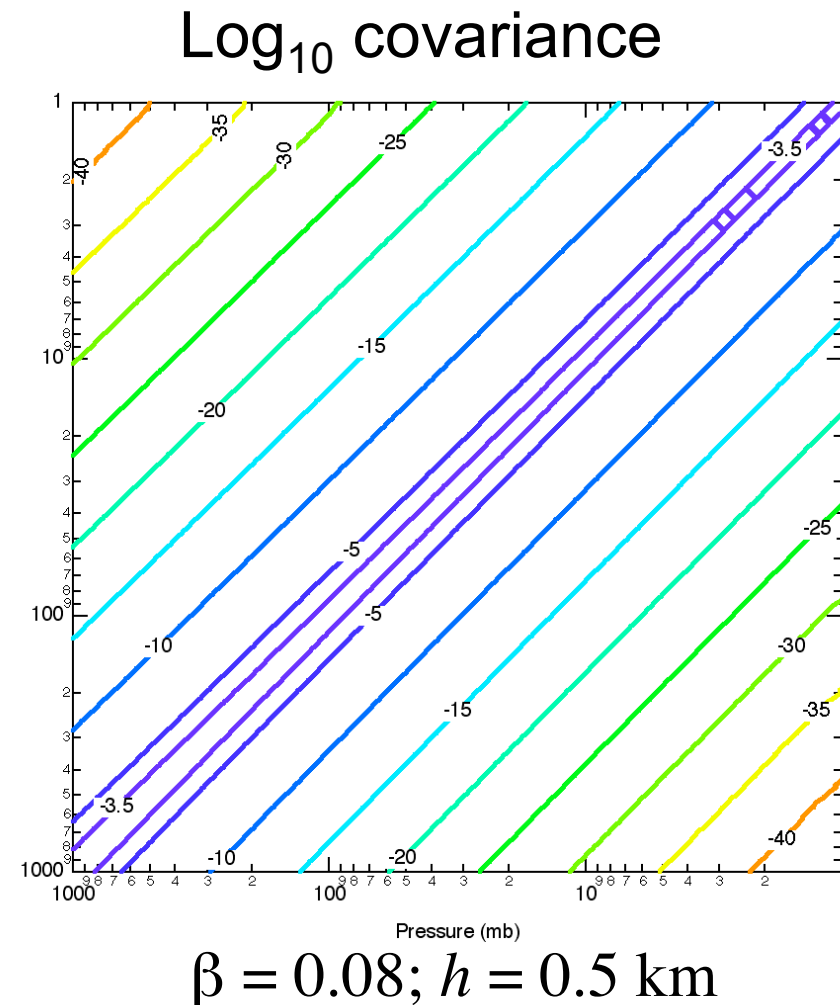
Off diagonals<sup>1</sup>:

$$S_{i,j} = S_{i,i} \exp \left( -|i - j| \frac{\delta z}{h} \right)$$

$h$  = off-diagonal length scale

Individual errors not rigorous  
because of ad hoc constraint

<sup>1</sup>per Rodgers [2000]





# Sample Averaging Kernel

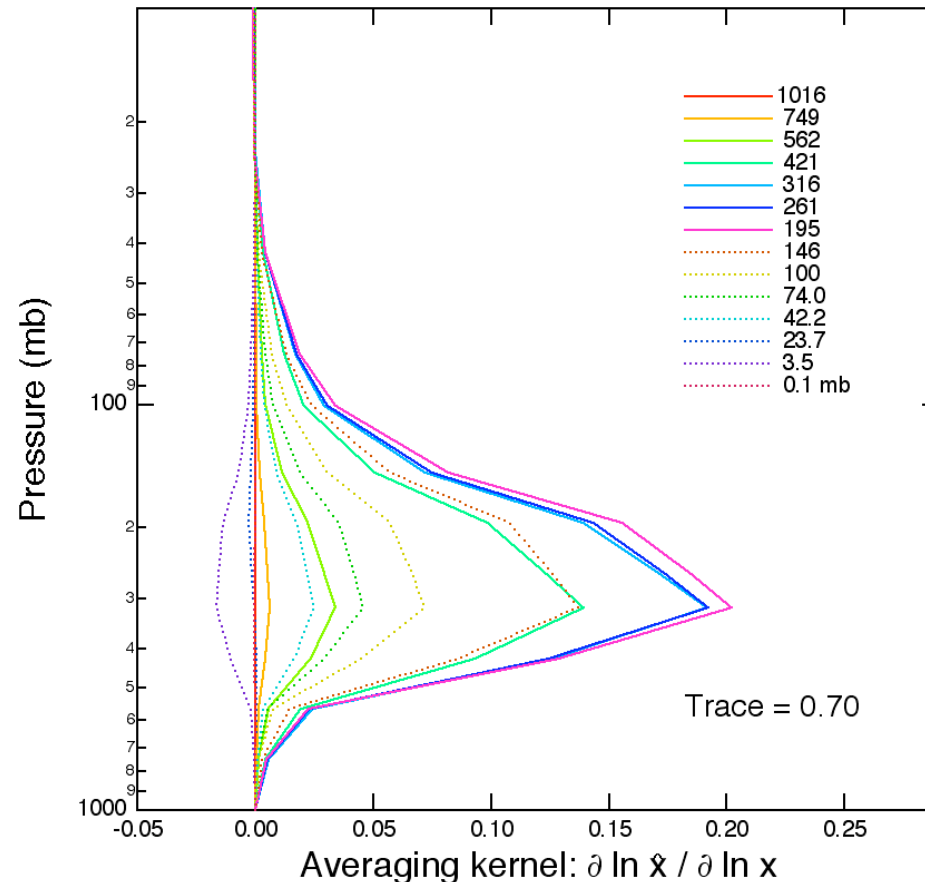
*Varies observation to observation*

Average channel SNR  
for this example = 114

Peak sensitivity from  
~200 to 400 mb

Diagonal of constraint  
matrix largely  
determines sensitivity.

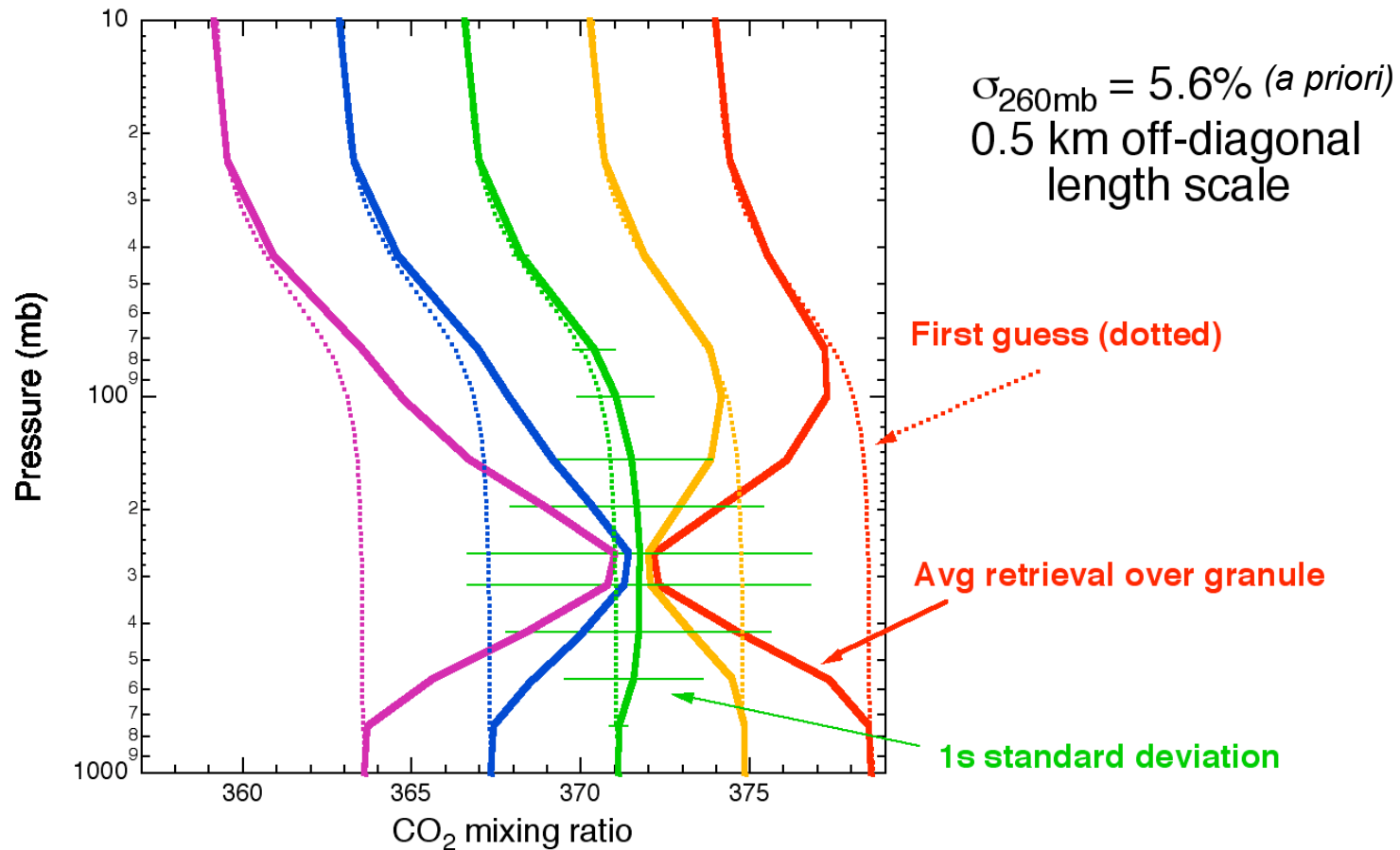
Off-diagonals  
determine resolution.



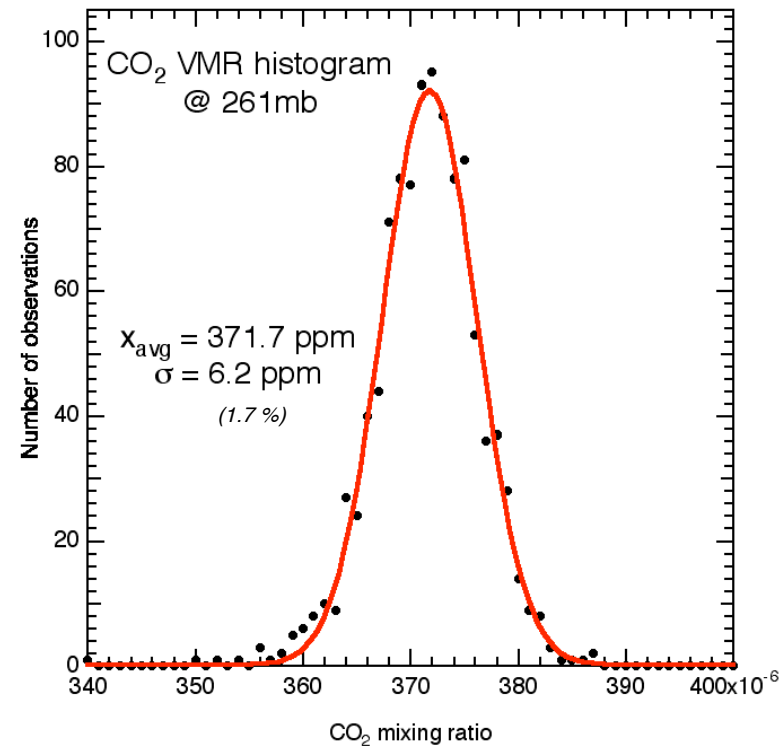
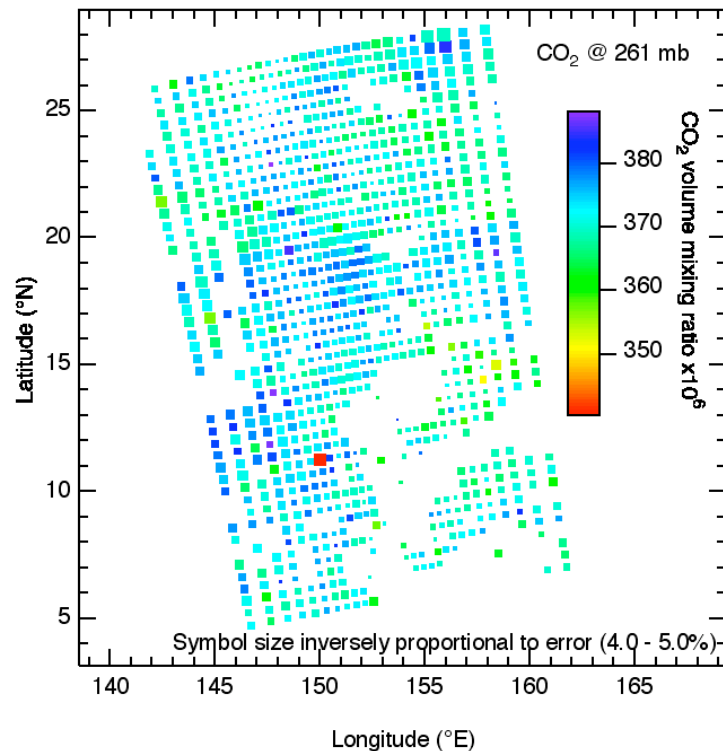
$h = 0.5 \text{ km}$ , a priori  $\sigma_{260\text{mb}} = 5.6\%$

# Average retrieval results over granule

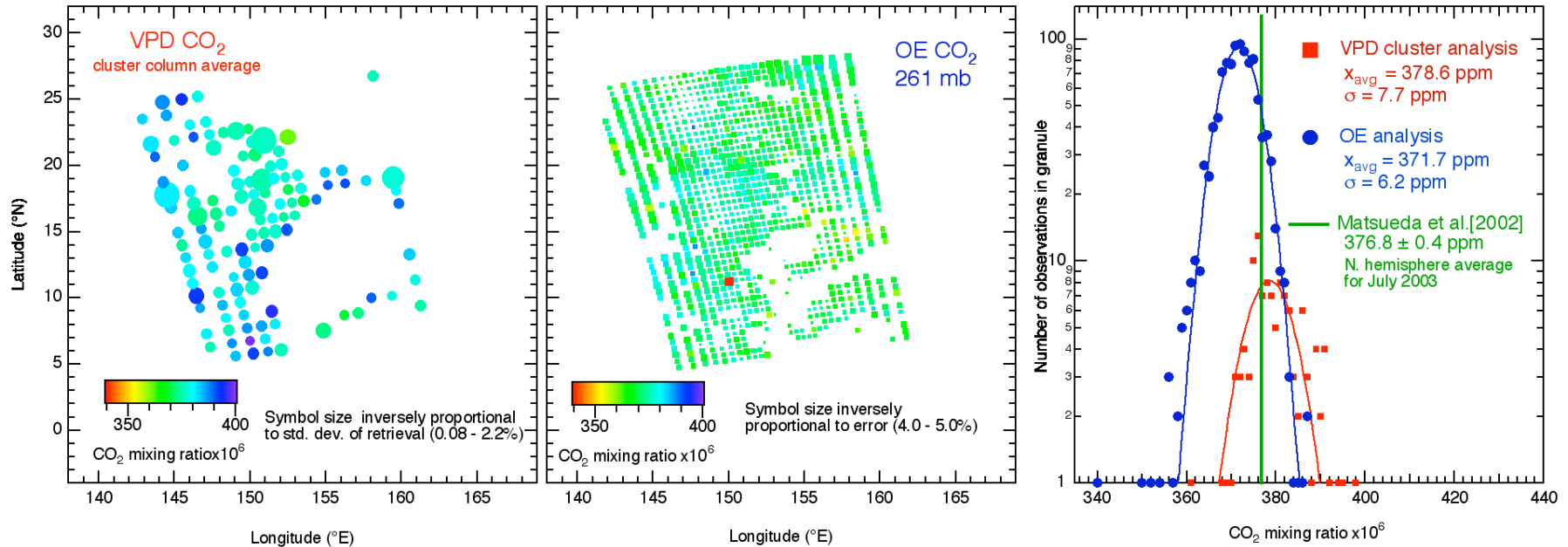
*Analysis over granule repeated five times using same constraint but different 1st guess profiles*



# Retrievals over granule @ 261 mb



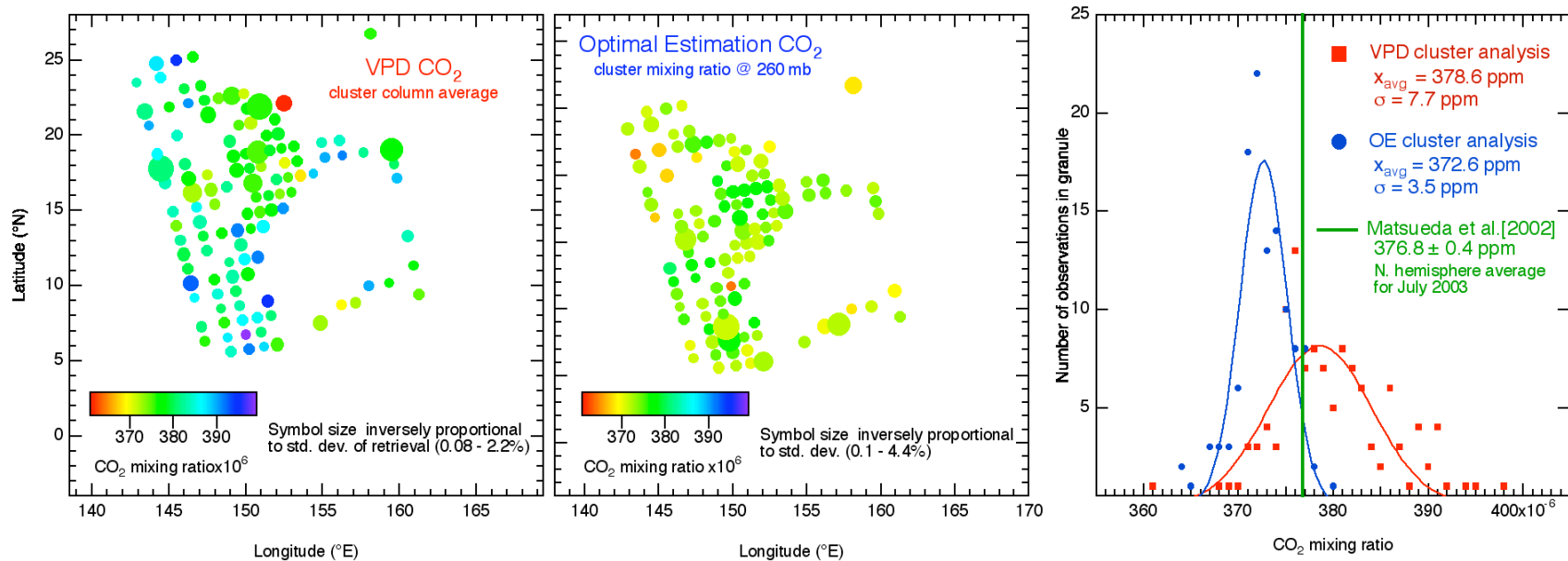
# Comparison to Vanishing Partial Derivatives



*Thanks to Luke Chen for VPD processing*

# Clustered comparison to Vanishing Partial Derivatives

Optimal Estimation retrievals filtered and averaged similar to VPD.



# Conclusions

- With OE, “loose” diagonal and low off-diagonals in a priori covariance give robust retrievals *in the aggregate*
- Comparable distribution of results to VPD
- Need to understand bias between OE and VPD results
  - Forward model (incl. spectroscopy differences)?
  - Temperature profile?
- Need to merge in AIRS forward model to increase speed of retrieval, and provide data on monthly timescales.

# Backup Slides

# Repeat the analysis with different covariance matrices

On the diagonal:

$$S_{i,i} = \left[ \ln \left( \frac{\beta - 0.01}{1 + 0.03(z/\delta z)} + 1.01 \right) \right]^2$$

$\beta$  is the fractional std. dev. at surface

$z$  = altitude

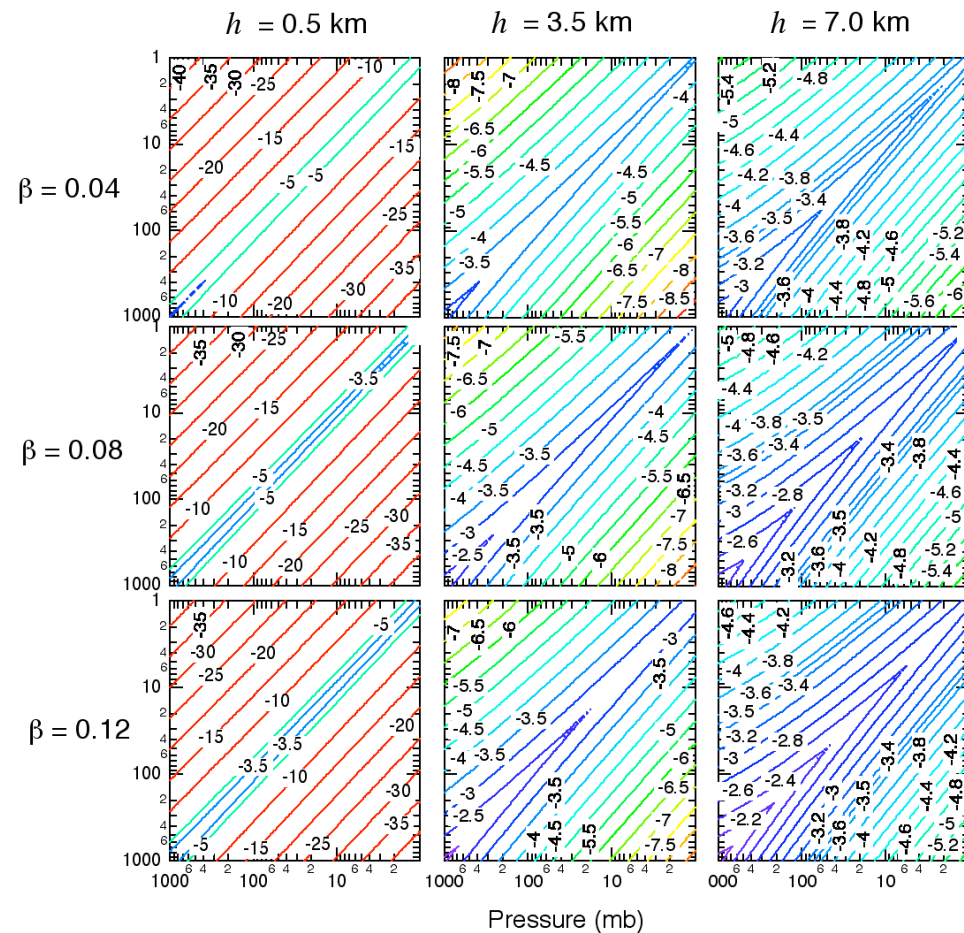
$\delta z$  = vertical spacing

Off diagonals:

$$S_{i,j} = S_{i,i} \exp \left( -|i - j| \frac{\delta z}{h} \right)$$

$h$  = off-diagonal length scale

Log<sub>10</sub> covariance





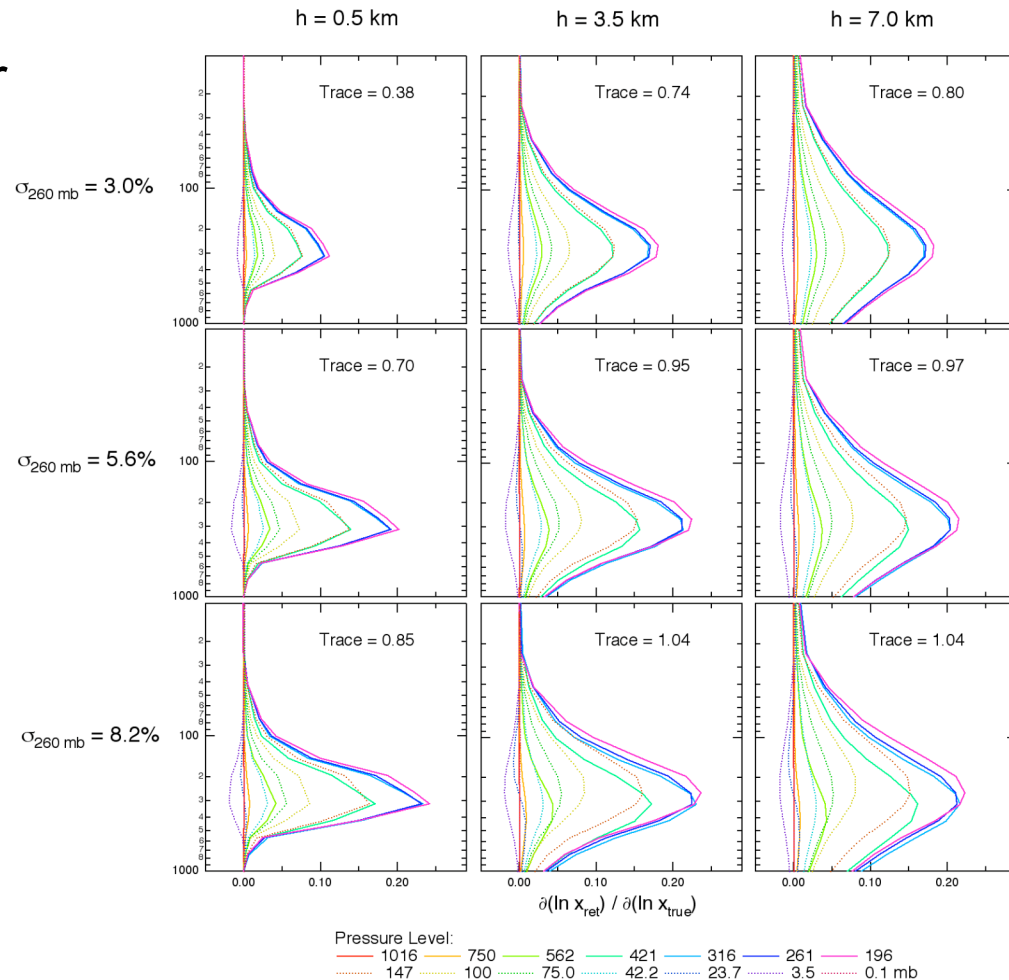
# Averaging kernels

Average channel SNR for  
this example = 114

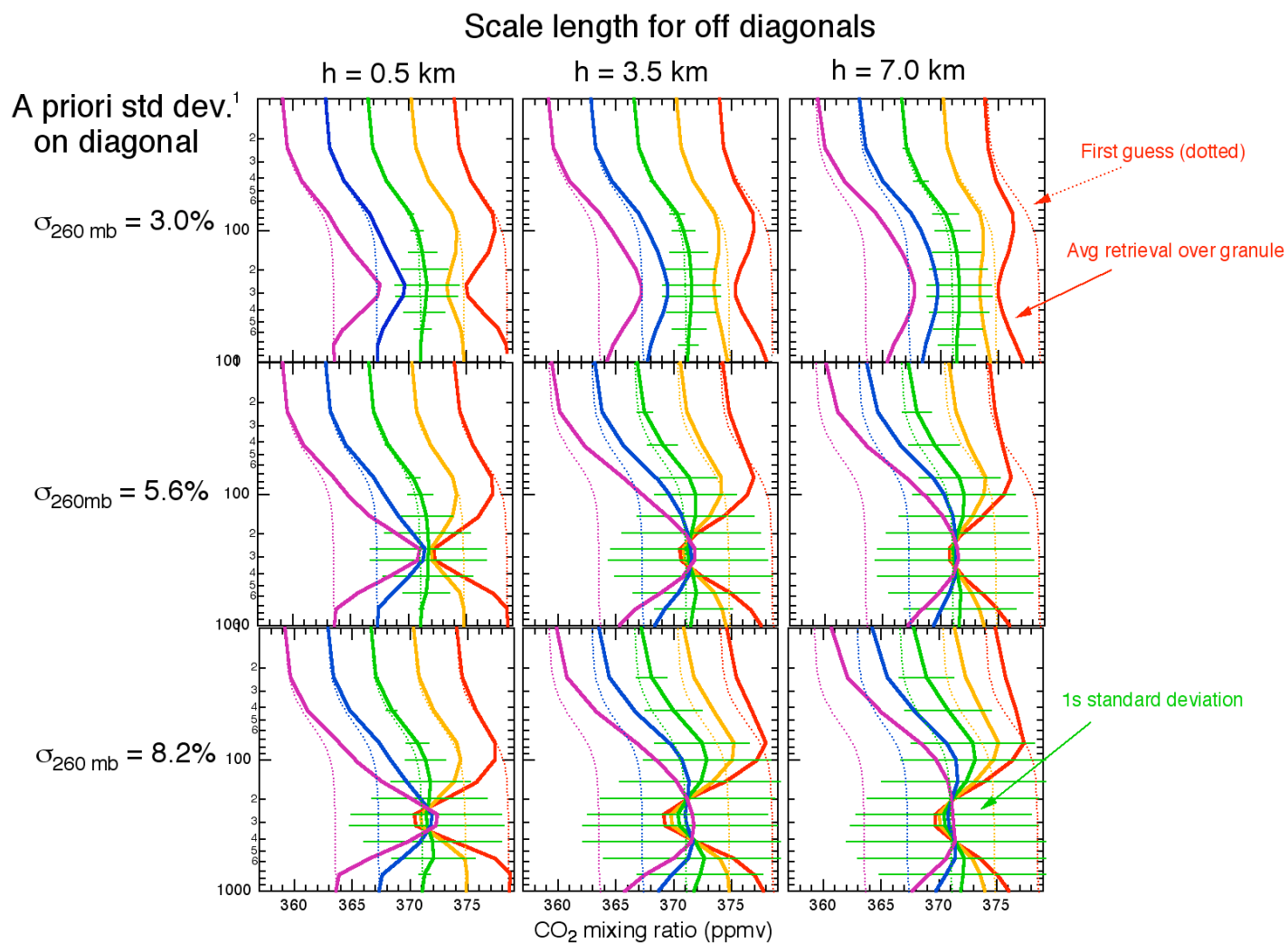
Peak sensitivity from  
~200 to 400 mb

Diagonal of constraint  
matrix largely  
determines sensitivity.

Off-diagonals  
determine resolution.



# Averaged results (all covar matrices)

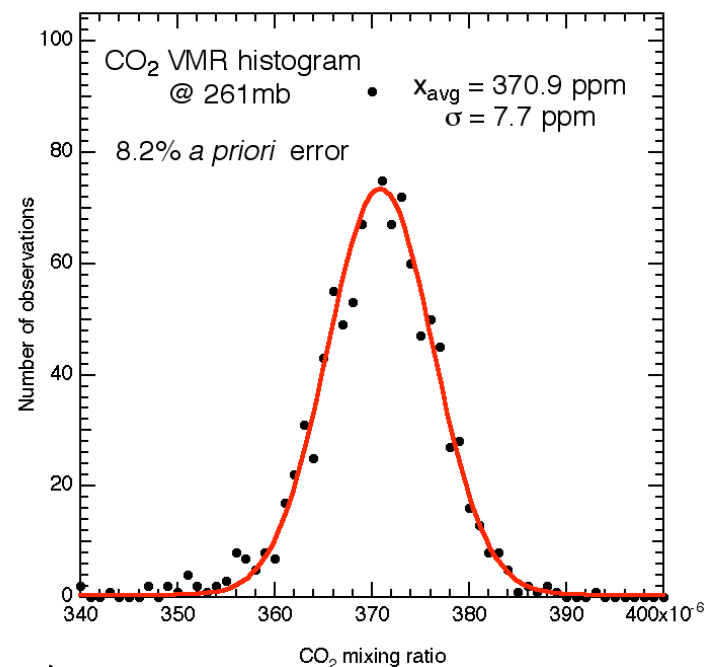
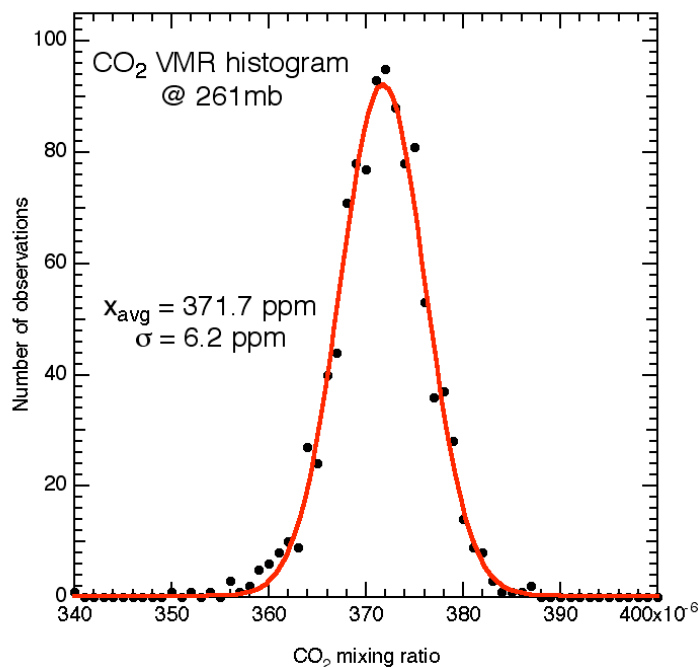


# Effect of “looser” constraint

5.6% *a priori*  
error at 260 mb

46%  
increase

8.2% *a priori*  
error at 260 mb



$\sigma = 1.7\%$

24% increase

$\sigma = 2.1\%$

No  
correlation  
between  
VPD and  
OE cluster  
results

